

Homework 2 in Cryptography II

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Exercise 4. Let $p > 2$ be prime. Let $\left(\frac{a}{p}\right)$ be the Legendre symbol. Prove the following calculation rules:

(a) $\left(\frac{-1}{p}\right) = (-1)^{\frac{p-1}{2}},$

(b) $\left(\frac{a}{p}\right) \left(\frac{b}{p}\right) = \left(\frac{ab}{p}\right),$

(c) $\left(\frac{a}{p}\right) = \left(\frac{b}{p}\right),$ if $a \equiv b \pmod{p}.$

Exercise 5. Show that Algorithm 6 from the lecture notes calculates the Jacobi symbol.

Exercise 6. Bob gets the message

(101010111000011010001011100101111100110111000, 1306)

from Alice. This message was encrypted with the Blum-Goldwasser Cryptosystem with the public key $n = 1333$. The number 1306 represents x_{10} . Decrypt this message.

Note: The security requirement to only use a maximum of $\log_2(\log_2(n))$ bits of the BBS generator is violated in this example. Instead, 5 bits of output are used.

Note: The letters of the alphabet A, \dots, Z are represented in the following way by 5 bits: $A = 00000, B = 00001, \dots, Z = 11001.$