

Es sei $1 \leq i \leq K-1$:

$$\begin{aligned}\tilde{\lambda}_i &= \tilde{\lambda}_i + \sum_{j=1}^K \tilde{\lambda}_j \tilde{r}_{ji} = \lambda_i + \sum_{j=1}^{K-1} \tilde{\lambda}_j \tilde{r}_{ji} + \tilde{\lambda}_K \tilde{r}_{Ki} \\ &= \lambda_i + \sum_{j=1}^{K-1} \tilde{\lambda}_j \tilde{r}_{ji} + \tilde{\lambda}_K \frac{\sum_{l=K}^J \lambda_l r_{li}}{\sum_{l=K}^J \lambda_l}\end{aligned}$$

$\tilde{\lambda}_i = \lambda_i$ einsetzen :

$$\begin{aligned}\lambda_i &= \lambda_i + \sum_{j=1}^{K-1} \lambda_j r_{ji} + \sum_{l=K}^J \lambda_l r_{li} \\ &= \lambda_i + \sum_{j=1}^J \lambda_j r_{ji} \quad \checkmark\end{aligned}$$

Es sei $i = K$:

$$\tilde{\lambda}_K = \tilde{\lambda}_K + \sum_{j=1}^K \tilde{\lambda}_j \tilde{r}_{jK}$$

$\tilde{\lambda}_K, \tilde{\lambda}_j$ einsetzen :

$$\begin{aligned}\sum_{l=K}^J \lambda_l &= \sum_{l=K}^J \lambda_l + \sum_{j=1}^{K-1} \left(\lambda_j \sum_{l=K}^J r_{lj} \right) + \\ &+ \left(\sum_{l=K}^J \lambda_l \right) \cdot \frac{\sum_{l=K}^J \left(\lambda_l \sum_{j=K}^J r_{lj} \right)}{\sum_{l=K}^J \lambda_l} \\ &= \sum_{l=K}^J \left(\lambda_l + \sum_{j=1}^J \lambda_j r_{jl} \right) \\ &= \sum_{l=K}^J \lambda_l \quad \checkmark\end{aligned}$$